

UNITED STATES PATENT APPLICATION

FOR

**METHOD, APPARATUS, AND SYSTEM FOR EFFICIENT RATE CONTROL  
IN AUDIO ENCODING**

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METHOD, APPARATUS, AND SYSTEM FOR EFFICIENT RATE CONTROL IN  
AUDIO ENCODING

## 5 FIELD OF THE INVENTION

The present invention relates to the field of signal processing. More specifically, the present invention relates to a method, apparatus, and system for efficient rate control in audio encoding.

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## BACKGROUND OF THE INVENTION

As technology continues to advance and the demand for video and audio signal processing continues to increase at a rapid rate, effective and efficient techniques for signal processing and data transmission have become more and more important in system design and implementation. Various standards or specifications for audio signal processing have been developed over the years to standardize and facilitate various coding schemes relating to audio signal processing. In particular, a group known as the Moving Pictures Expert Group (MPEG) was established to develop a standard or specification for the coded representation of moving pictures and associated audio stored on digital storage media. As a result, a standard known as the

ISO/IEC 11172-3 (Part 3 - Audio) CODING OF MOVING PICTURES AND ASSOCIATED AUDIO FOR DIGITAL STORAGE MEDIA AT UP TO ABOUT 1.5 MBITS/S (also referred to as the MPEG standard or MPEG specification herein), published August, 1993, was developed which standardizes various coding schemes for audio signals, e.g., MPEG-1 or MPEG-2 Layers I, II, and III. ISO stands for International Organization for Standardization and IEC stands for International Electrotechnical Commission, respectively. Generally, the MPEG audio specification does not standardize the encoder but rather the type of information that an encoder needs to produce and write to an MPEG compliant bitstream, as well as the way in which the decoder needs to parse, decompress, and resynthesize this information to regain the encoded audio signals. In particular, MPEG standard is developed for perceptual audio coding rather than lossless coding. In lossless coding, redundancy in the waveform is reduced to compress the sound signal and the decoded sound wave does not differ from the original sound wave. In contrast, in perceptual audio coding, the aim is not to regain the original signal exactly after encoding and decoding but rather to eliminate those parts of the audio signal that are irrelevant to the human ear (e.g., that are not heard).

An audio encoder typically includes a bit allocation module or unit (also called the bit allocator herein) whose role is to allocate more bits to those frequencies where quantization noise is audible to a listener and allocate  
5 fewer bits to those frequencies where quantization noise is masked and is inaudible to the listener. Also, the bit allocator needs to ensure that the total number of bits used for a specific audio block or frame does not exceed the maximum number of bits available as determined by the  
10 specified output bit rate. Currently, the methods for performing the bit allocation, as described in the MPEG standard includes two processing loops: (1) an outer or distortion control loop; and (2) an inner or rate control loop. One of the problems or disadvantages associated with  
15 the current methods described in the ISO/IEC 11272-3 MPEG standard is their inefficiency due to numerous iterations involved in determining or computing the optimum quantization parameters that will satisfy the rate criteria.

**BRIEF DESCRIPTION OF THE DRAWINGS**

The features of the present invention will be more fully understood by reference to the accompanying drawings, in which:

5        Figure 1 is a block diagram of one embodiment of an encoder in which the teachings of the present invention may be implemented;

      Figure 2 is a flow diagram illustrating an inner or rate control loop of a bit allocation method according to  
10    the current ISO/IEC specification;

      Figure 3 shows a flow diagram illustrating an outer or distortion control loop of a bit allocation method according to the current ISO/IEC specification;

      Figures 4, 5, and 6 illustrate examples of the  
15    progression from an initial global gain value to a final global gain value, in accordance with one embodiment of the present invention;

      Figure 7 shows an example of a curve where the estimation of the global\_gain leads to a value of the  
20    total\_bits that is below but not close to the target\_bits;

      Figure 8 shows a flow diagram of one embodiment of a rate control process according to the teaching of the present invention; and

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Figure 9 shows a flow diagram of a process in accordance with one embodiment of the present invention.

**DETAILED DESCRIPTION**

In the following detailed description numerous specific details are set forth in order to provide a thorough understanding of the present invention. However, 5 it will be appreciated by one skilled in the art that the present invention may be understood and practiced without these specific details. Furthermore, while the teachings of the present invention are applicable to MPEG Layer III (commonly known as MP3) audio encoding, it should be 10 appreciated and understood by one skilled in the art that the present invention is not limited to MPEG Layer III audio encoding and can be applied to any method, apparatus, and system for efficient bit allocation to accomplish bit rate reduction in audio processing.

15 Figure 1 is a block diagram of one embodiment of an encoder 100 in which the teachings of the present invention may be implemented. In one embodiment, the audio encoder 100 may include a filter bank structure or unit 110, a psycho-acoustic model (PAM) 120, a bit allocator and 20 quantizer 130, a Huffman encoder 140, and a bitstream formatter 150. In one embodiment, input audio samples such as pulse code modulation (PCM) samples are fed into the filter bank unit 110 and transformed using a filter bank to generate output sub-band samples. In MP3 audio encoding,

the output sub-band samples can be further processed using a Modified Discrete Cosine Transform (MDCT) to obtain higher frequency resolution. The input PCM samples are also input to the Psycho-Acoustic model 120, which independently  
5 analyzes the input data and models human auditory perception. The psycho-acoustic model 120 is designed and configured to determine the ear sensitivity to noise in the frequency domain. In one embodiment, the output from the psycho-acoustic model 120 is a frequency mask that  
10 describes the maximum allowed quantization noise in each of the bands. Both the MDCT output spectrum and the frequency mask are then input into the bit allocator and quantizer 130. The function of the bit allocator (also called bit allocation module herein) in block 130 is to allocate more  
15 bits to those frequencies where quantization noise is audible to the listener and allocate fewer bits to frequencies where quantization noise is masked by program material and is inaudible to the listener. Furthermore, the bit allocator needs to ensure that the total number of bits  
20 used for a specific PCM block (or frame) does not exceed the maximum number of bits available as determined by the specified output bit rate. The output generated from the bit allocator and quantizer 130 is then input into the Huffman encoder 140. The bitstream formatter 150 is



configured to generate output encoded audio frames based on the data received from the Huffman encoder 140.

Figure 2 is a flow diagram illustrating an inner or rate control loop of a bit allocation method according to the current ISO/IEC specification. Generally, the rate control loop is responsible for selecting a *global\_gain* value (also called the quantizer step size value herein) to insert in the following quantization formula:

$$ix(i) = \text{nint} \left[ \left( \frac{|x_r(i)|}{2^{\frac{\text{global\_gain}}{4}}} \right)^{3/4} + 0.0946 \right] \quad (1)$$

where *ix* corresponds to the quantized spectral values for frequency line *i*, and *xr* corresponds to the original spectral value. Since the quantized values will be further encoded using Huffman tables, the *global\_gain* parameter first is adjusted so that the maximum quantized value falls below the maximum limit of the corresponding Huffman lookup tables described in ISO/IEC specification. This is done according to the ISO/IEC spec by continuously increasing the *global\_gain* value until the maximum quantized value is less or equal to the maximum Huffman lookup table (LUT) index (e.g. 8191 for MP3 encoding). After selecting the

minimum *global\_gain* to allow Huffman table look-up, the next task is to ensure that the number of bits used for Huffman encoding does not exceed the maximum number of bits allocated for the block of spectral values. This is done according to the ISO/IEC spec by continuously increasing the *global\_gain* value until the number of bits used for encoding is equal or less than the maximum number of bits allocated for the block. As shown in Figure 2, at block 210, the *global\_gain* value is initially set to zero or to some initial estimate. At block 215, the spectral values are quantized. At decision block 220, if the maximum quantized spectral value is within the corresponding Huffman table limit, then the process continues to block 225, otherwise the process proceeds to block 230. At block 230, the value of the *global\_gain* is increased (e.g., incremented by 1) and the process loops back to block 215. At block 225, a number of bits used for Huffman encoding is determined. At decision block 235, if the number of bits used for Huffman encoding exceeds the maximum number of bits allocated for the block of spectral values, then the process proceeds to block 240 to increase the value of the *global\_gain* (e.g., increment the value of the *global\_gain* by 1), otherwise the process proceeds to end at block 290.

At block 245, the spectral values are quantized. The process then loops back from block 245 to block 225.

Figure 3 shows a flow diagram illustrating an outer or distortion control loop of a bit allocation method according to the current ISO/IEC specification. Generally, after determining a *global\_gain* value to meet the rate criteria as described above, the outer or distortion control loop computes the amount of distortion introduced by the quantization. This is accomplished by decoding the quantized value and finding the mean-squared error (MSE), or some other distortion measure, between the decoded spectral value and the original spectral value within each *scalefactor* band (group of frequency lines). Scalefactor bands not meeting the distortion criteria are amplified by some prescribed factor and the rate control loop is called iteratively with the new amplified spectral values, until the distortion criteria is met for all the bands. As shown in Figure 3, at block 310 the rate control loop as described in Figure 2 is called to determine a *global\_gain* value. At block 315, for each scalefactor band, the process proceeds as follows. At block 320, the distortion for the respective band is calculated. At decision block 325, if the distortion calculated does not meet the distortion criteria (e.g., the distortion calculated is not

less than the maximum distortion allowed) then the process proceeds to block 330 to amplify the respective band by a predetermined factor. At decision block 335, if the distortion criteria is met for all the bands (e.g., no  
5 distorted bands), then the process proceeds to end at block 390. Otherwise the process loops back to block 310.

As mentioned above, a disadvantage associated with the methods disclosed in the ISO/IEC document is their inefficiency due to the numerous iterations involved in  
10 computing the *global\_gain* value to satisfy the rate criteria.. As described in more details below, according to the teachings of the present invention, a new method is provided for efficient bit allocation of spectral values obtained from a sub-band filter. In one embodiment of the  
15 present invention, the method as described herein is directed to improving the efficiency of the rate control loop (also called rate control process herein). The method as described herein includes the following:

- Deriving a closed form equation to determine the  
20 *global\_gain* to meet the maximum Huffman look-up limit; and
- Using a modified Newtonian search to determine the *global\_gain* required to meet the rate criteria.

Accordingly, at a high level, the present invention includes two parts or two components as follows: (1)

efficient determination of a minimum *global\_gain* value to meet the maximum Huffman look-up criteria; and (2) efficient determination of a *global\_gain* value to meet the rate criteria within the rate control loop.

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Determining the minimum *global\_gain* value to meet the maximum Huffman look-up criteria

Huffman tables that are used in a typical audio encoder are limited to a maximum quantized value that can be looked up using the table index. For example, Huffman tables that are used in a typical MP3 encoder are limited to a maximum quantized value of 8191 that corresponds to 13 bits of precision ( $2^{13}$  entries). Therefore, the maximum quantized value for the block of spectral values needs to be bounded to the maximum index into the corresponding Huffman tables. For illustration and generalization purposes, the maximum quantized value is called  $\alpha$ . In the case of MP3 encoding,  $\alpha = 8191$ . Equation (2) below can be obtained using equation (1) shown above:

$$ix(i) = \text{nint} \left[ \left( \frac{|x_r(i)|}{\frac{\text{global\_gain}}{2^4}} \right)^{3/4} + 0.0946 \right] \leq \alpha \quad (2)$$

Removing the `nint[]` function (standing for nearest integer), the following equation (3) can be obtained:

$$\left( \frac{|x_r(i)|}{2^{\frac{\text{global\_gain}}{4}}} \right)^{3/4} + 0.0946 + \varepsilon \leq \alpha \quad (3)$$

where  $\varepsilon$  is the error introduced by quantizing to the nearest integer, and therefore:

$$|\varepsilon| \leq 0.5 \quad (4)$$

5 In one embodiment, using  $\varepsilon = 0.5$  and setting  $|x_r(i)| = \text{MAX}|x_r(i)|$  will result in the largest value for the left hand side of equation (3), where  $\text{MAX}|x_r(i)|$  represents the largest spectral value magnitude across the frequency lines indexed by  $i$ . Therefore, equation (3) can be re-written as:

$$10 \quad \left( \frac{\text{MAX}|x_r(i)|}{2^{\frac{\text{global\_gain}}{4}}} \right)^{3/4} + 0.0946 + 0.5 \leq \alpha \quad (5)$$

The following equations (6)-(10) are used to solve equation (5) for the variable  $\text{global\_gain}$ . Equation (5) can be rewritten as follows:

$$\left( \frac{\text{MAX}|x_r(i)|}{2^{\frac{\text{global\_gain}}{4}}} \right)^{3/4} \leq \alpha - 0.5946 \quad (6)$$

15 Taking the  $4/3$  root on both sides of equation (6), equation (7) is obtained as shown below:

$$\frac{\text{MAX}|x_r(i)|}{2^{\frac{\text{global\_gain}}{4}}} \leq [\alpha - 0.5946]^{4/3} \quad (7)$$

Solving for  $2^{\text{global\_gain}/4}$  results in the following equation:

$$2^{\frac{\text{global\_gain}}{4}} \geq \frac{\text{MAX}|x_r(i)|}{[\alpha - 0.5946]^{4/3}} \quad (8)$$

Taking the logarithm base 2 of both sides of equation (7), the following equation is obtained:

$$\frac{\text{global\_gain}}{4} \geq \log_2 \left( \frac{\text{MAX}|x_r(i)|}{[\alpha - 0.5946]^{4/3}} \right) \quad (9)$$

Solving for global\_gain results in equation (10) shown below:

$$\text{global\_gain} \geq 4 \cdot \log_2 \left( \frac{\text{MAX}|x_r(i)|}{[\alpha - 0.5946]^{4/3}} \right) \quad (10)$$

Since global\_gain needs to be an integer number, take the ceiling of equation (10) to obtain the following equation:

$$\text{global\_gain} \geq \left\lceil 4 \cdot \log_2 \left( \frac{\text{MAX}|x_r(i)|}{[\alpha - 0.5946]^{4/3}} \right) \right\rceil \quad (11)$$

where  $\lceil x \rceil$  corresponds to the nearest integer that is greater than or equal to  $x$ . Therefore, the minimum global\_gain value required to meet the maximum Huffman table entry  $\alpha$ , can be computed from equation (11).

Efficient determination of a global gain value to meet the rate criteria

In one embodiment of the present invention, a modified Newtonian search process or algorithm is developed as described in more details below to find the roots of the following equation:

$$5 \quad \text{total\_bits} = f_{\text{Huffman}}(ix) = f_{\text{Huffman}}(\text{global\_gain}) \leq \text{target\_bits} \quad (12)$$

where  $f_{\text{Huffman}}(.)$  corresponds to the total number of bits used during Huffman encoding of the quantized values  $ix$ , which as shown in equation (12) is a function of  $\text{global\_gain}$ . The value  $\text{target\_bits}$  correspond the maximum number of bits to  
 10 be encoded per audio frame. In one embodiment, this value is dependent on a desired compression ratio or output bit rate and the input audio frame. For example, in MP3 encoding, the input audio frames include 1152 PCM samples per channel. If the input sampling rate of the audio signal  
 15 is 44.1KHz (or 44100 samples/sec), and the encoding is to be done at 128 Kbits/sec, then the  $\text{target\_bits}$  for one channel of an audio frame can be computed as follows:

$$\text{target\_bits} = \frac{128000\text{bits/sec} \cdot 1152\text{samples}}{44100\text{samples/sec}} - \langle \text{bits used for MP3 header} \rangle$$

In general, a Newtonian search process works by  
 20 calculating the line tangent to an "unknown" surface and using the intercept of this line as a new guess for the root of the surface or function.



Figures 4, 5, and 6 illustrate examples of a progression from an initial global\_gain value, gg0, towards a final global\_gain, gg4, that satisfies the condition in equation (12), according to the teachings of the present invention. In one embodiment, linear convergence faster than the ISO/IEC method or ISO/IEC algorithm is achieved by using the x intercept to determine a new global\_gain, which yields a bit allocation value closer to target\_bits.

Generally, the Newton search algorithm or process is a special case of a class of root finding techniques based on Nth-order polynomials. Specifically, the Newton search corresponds to a 1<sup>st</sup> order polynomial. This root finding technique derives from the Taylor Series of a function f(x) at some  $\delta$  interval from x as follows:

$$f(x+\delta) = f(x) + f'(x)\delta + f''(x)\frac{\delta^2}{2} + \dots + f^n(x)\frac{\delta^n}{n!} + \dots \quad (13)$$

where  $f^n(x)$  corresponds to the  $n^{\text{th}}$  derivative of function f(x).

For relatively smooth functions, derivatives of 2<sup>nd</sup> order and above may be negligible, and therefore,  $f(x+\delta)$  may be approximated by:

$$f(x+\delta) \approx f(x) + f'(x)\delta \quad (14)$$

In trying to find the value of  $x$  for which the function is equal to some value  $c$ , set  $f(x+\delta) = c$ , and obtain the following:

$$\delta \approx \frac{c - f(x)}{f'(x)} \quad (15)$$

5 Equation (15) corresponds to the Newton approximation. For the bit allocation problem as described herein,  $x$  is substituted with the `global_gain`;  $f(x)$  is substituted with the total Huffman bits,  $f_{\text{Huffman}}(\text{global\_gain})$ ;  $c$  is the desired root, in this case `target_bits`; and  $\delta$  corresponds to  
 10 the step size to be used to obtain a new `global_gain`. For clarity purposes, the  $f(\text{global\_gain})$  is used to represent  $f_{\text{Huffman}}(\text{global\_gain})$  from now on. Therefore, equation (15) becomes:

$$\delta_{\text{global\_gain}} \approx \frac{\text{target\_bits} - f(\text{global\_gain})}{f'(\text{global\_gain})} \quad (16)$$

15 The derivative,  $f'(\text{global\_gain})$ , at iteration  $i$ , can be numerically approximated as follows:

$$f'(\text{global\_gain}_i) \approx \frac{f(\text{global\_gain}_i) - f(\text{global\_gain}_{i-1})}{\text{global\_gain}_i - \text{global\_gain}_{i-1}} \quad (17)$$

The estimation of the function's derivative uses the previously computed `global_gain`. This estimation of the  
 20 derivative is sometimes called in literature as the Secant method for finding roots. Generally, this technique is

simple and works well with well-behaved functions as in the case of Huffman tables. However, it should be understood and appreciated by one skilled in the art that any derivative estimation technique can be used in accordance with the teachings of the present invention.

In one embodiment, the assumption in the use of a 1<sup>st</sup> order polynomial is that the function to be searched is relatively smooth and its derivative is close to a straight line. For example, the Huffman tables used for MPEG encoding are designed so that the total number of bits decreases progressively towards 0 as the `global_gain` is increased. Therefore, this implies that the function  $f(\text{global\_gain})$  is well behaved, and a 1<sup>st</sup> order polynomial will suffice. In one embodiment, the straight line for the derivative is then used to estimate a new `global_gain`, i.e., `global_gainn+1`.

Two issues may arise when using a Newtonian search with equation (12):

- First, a large step size in the `global_gain` value will cause the algorithm to converge rapidly. However, the `global_gain` estimation should be as close as possible to the `target_bits`. Figure 7 shows an example of a curve where the estimation of the `global_gain` leads to a value of the `total_bits` that is below the `target_bits`. However,

this is not the closer one to the target\_bits, and hence, it is non-optimal.

◦ Second, since global\_gain needs to be an integer value, the global\_gain value gets truncated to the closer integer that is less than or equal to the obtained global\_gain during each iteration. As the search progresses in the iterations and gets closer to target\_bits, the step size for estimating the new global\_gain may be less than 1, which means that global\_gain will not change and therefore the process would enter a non-convergent cycle.

In one embodiment of the present invention, the first issue was addressed by allowing the search process to back-track to a smaller value of global\_gain after it reaches a global\_gain that satisfies the condition in equation (12). In one embodiment, this back-tracking can be repeated more than once. Then, the global\_gain that results in a total\_bits closer to target\_bits is selected. Usually, the selection may not be necessary, since the last global\_gain after N times is the closer one to the target\_bits. The times the process is allowed to reach a total\_bits that satisfies equation (12) is denominated as "go\_up" in the flow diagram shown in Figure 8 described below.

In one embodiment, the second issue was addressed by forcing the global\_gain during each iteration to be updated

by at least a positive integer (e.g., +1) or a negative integer (e.g., -1), depending on the direction of the search. A positive integer such as +1 is used if the process is still progressing down towards target\_bits, and  
 5 a negative integer such as -1 is used when the process reaches a total\_bits below target\_bits and the search is continued.

In one embodiment of the present invention, the global\_gain parameter is stored in memory to be used as an  
 10 initial estimate for the next block of spectral values. Two initial values of total\_bits ( $tb_0$  and  $tb_1$ ) computed from two initial global\_gains ( $gg_0$  and  $gg_1$  respectively) are used to start the iteration. In one embodiment,  $gg_0$  is taken as the global\_gain pre-computed as described above and  $gg_1$  can be  
 15 computed as follows:

$$gg_1 = \max(gg_0 + \beta, \text{global\_gain from previous block}) \quad (18)$$

where  $\beta$  can be a predetermined positive integer that can be optimized to increase the convergence rate. For example, a value of 5 for  $\beta$  can be used. In one embodiment, the  
 20 global\_gain of the previous block is compared with  $gg_0$  to ensure that the criteria of equation (11) is met for  $gg_1$ .

Figure 8 shows a flow diagram of one embodiment of a rate control process (also called rate control loop) 800

according to the teaching of the present invention. At block 810, a first initial value of the `global_gain` parameter (e.g., `gg0`) is computed. In one embodiment, the first initial value `gg0` is computed using equation (11) as described above. At block 812, a second initial value of the `global_gain` parameter (e.g., `gg1`) is computed, based on equation (18) as described above. At block 814, the spectral values are quantized using `gg0`. At block 816, a first initial value for the `total_bits` parameter is computed. In one embodiment, the first initial value for the `total_bits` is computed based on the Huffman encoding bits for `gg0`. At decision block 818, if the first initial value of the `total_bits` `tb0` is below the `target_bits` value then the process proceeds to end at block 890. Otherwise, the process proceeds to block 820 to quantize the spectral values using `gg1`. At block 822, a second initial value of the `total_bits` is computed. In one embodiment, the second initial value of the `total_bits` is computed using the Huffman encoding bits for `gg1`. At decision block 824, if the second initial value of the `total_bits` is below the `target_bits` value then the process proceeds to block 826, otherwise the process proceeds to block 828. At block 826, increase the number of iterations `go_up` (e.g., increment `go_up` by 1) and set the direction to back track to a

smaller value of `global_gain` (e.g., `direction = -1`). At block 828, since the current value of the `total_bits` is not below the `target_bits` value, set the direction to progress down towards the `target_bits` (e.g., `direction = 1`). The process then proceeds either from block 826 to block 830 or from block 828 to block 832. At block 830, if the maximum number iterations is reached (e.g., `go_up > max_go_up`), then the process proceeds to end at block 890, otherwise the process proceeds to block 832. At block 832, two new initial values of the `global_gain` parameter are computed for another iteration, based on the previous values of the `global_gain`, the previous values of the `total_bits`, and the `target_bits` value. The process then loops back from block 832 to block 820 to continue the search for the desired `global_gain` value.

Figure 9 shows a flow diagram of a process in accordance with one embodiment of the present invention. At block 910, audio samples (e.g., PCM samples) representing an input audio signal are received. At block 920, the input audio samples are transformed into a vector of spectral values in a frequency domain. At block 930, a value of a quantizing parameter that satisfies one or more criteria is determined, based at least in part, on a modified Newtonian search process. The determined value of

the quantizing parameter is used to quantize the respective vector of spectral values to generate a vector of quantize values.

As described above, several other root finding techniques can also be used in place of the Newtonian search. The theory behind some of the various techniques is discussed below.

#### Higher Order Polynomials

Higher order polynomials may be used to estimate the root of the function. For an Nth order polynomial, equation (13) is truncated after the N<sup>th</sup> derivative. For example, a 2<sup>nd</sup> order polynomial will correspond to:

$$f(x + \delta) = f(x) + f'(x)\delta + f''(x)\frac{\delta^2}{2} \quad (19)$$

In order to obtain the value of  $\delta$  that will satisfy the root condition, the following quadratic equation needs to be solved:

$$c = f(x) + f'(x)\delta + f''(x)\frac{\delta^2}{2} \quad (20)$$

Also, it is required to estimate the 2<sup>nd</sup> derivative of the function  $f(x)$ . If equation (17) is used to estimate the 2<sup>nd</sup> derivative, the following is obtained:

$$f''(\text{global\_gain}_i) \approx \frac{f'(\text{global\_gain}_i) - f'(\text{global\_gain}_{i-1})}{\text{global\_gain}_i - \text{global\_gain}_{i-1}} \quad (21)$$

which requires storing of the derivative at iteration  $i-1$ .



The technique of using a 2<sup>nd</sup> order polynomial, and using equation (21) to estimate the 2<sup>nd</sup> derivation of the function is commonly known in the art as the Muller's method.

## 5 Initial global gain Estimation

In one embodiment of the present invention, more than one global\_gain values are stored in memory for the estimation of the initial Newton search conditions. In one embodiment, gg<sub>0</sub> is computed according to equation (11) and  
10 gg<sub>1</sub> is computed according to the following equation:

$$gg_1^m = \max \left( gg_0^m + \beta, c_0 + \sum_k c_k \cdot \text{global\_gain}^k, k = m-1, m-2, \dots, m-N \right) \quad (22)$$

where m corresponds to the current audio frame under iteration and c<sub>k</sub> are empirically determined coefficients. The coefficients c<sub>k</sub> could be determined by executing a  
15 regression of global\_gain in audio frame m against the global\_gain values from the previous N frames. Any other error minimization technique could also be used to estimate the global\_gain coefficients.

The invention has been described in conjunction with  
20 the preferred embodiment. It is evident that numerous alternatives, modifications, variations and uses will be apparent to those skilled in the art in light of the foregoing description.